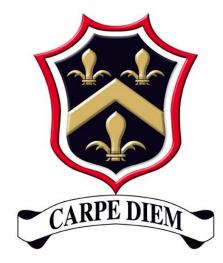
Maths Summer Homework



Year 11 to Year 12 Transition Support

It's a long summer! Working through these questions before you come back in September will give you the best possible start to your Year 12 maths studies at JKHS.

We suggest doing them in August, so they'll be fresh in your mind when you start here.

There are notes to help and the answers are at the end so you know if you got them right. If you're stuck or made an error there are mathswatch links to help you (username: a.guest@jkhs password: johnkyrle)

Chapter 1: REMOVING BRACKETS

To remove a single bracket, we multiply every term in the bracket by the number or the expression on the outside:

Examples

$$3(x + 2y) = 3x + 6y$$

2)
$$-2(2x-3) = (-2)(2x) + (-2)(-3)$$
$$= -4x + 6$$

To expand two brackets, we must multiply everything in the first bracket by everything in the second bracket. We can do this in a variety of ways, including

- * the smiley face method
- * FOIL (Fronts Outers Inners Lasts)
- * using a grid.

Examples:

1)
$$(x+1)(x+2) = x(x+2) + 1(x+2)$$

or
$$(x+1)(x+2) = x^2 + 2 + 2x + x$$

= $x^2 + 3x + 2$

or

	X	1	
х	<i>X</i> 2	X	
2	2x	2	

$$(x+1)(x+2) = x_2 + 2x + x + 2$$

= $x_2 + 3x + 2$

2)
$$(x-2)(2x+3) = x(2x+3) - 2(2x+3)$$

$$= 2x^2 + 3x - 4x - 6$$

$$= 2x^2 - x - 6$$

or
$$(x-2)(2x+3) = 2x_2-6+3x-4x = 2x_2-x-6$$

or

	x	-2
2x	$2x_{2}$	-4 <i>x</i>
3	3r	-6

$$(2x+3)(x-2) = 2x_2 + 3x - 4x - 6$$

= $2x_2 - x - 6$

EXERCISE A

Multiply out the following brackets and simplify.

- 1. 7(4x + 5)
- 2. -3(5x 7)
- 3. 5a 4(3a 1)
- 4. 4y + y(2 + 3y)
- 5. 3x (x + 4)
- 6. 5(2x-1)-(3x-4)
- 7. (x+2)(x+3)
- 8. (t-5)(t-2)
- 9. (2x + 3y)(3x 4y)
- 10. 4(x-2)(x+3)
- 11. (2y 1)(2y + 1)
- 12. (3 + 5x)(4 x)

Two Special Cases

Perfect Square:

$$(x + a)^2 = (x + a)(x + a) = x^2 + 2ax + a^2$$

 $(2x - 3)^2 = (2x - 3)(2x - 3) = 4x^2 - 12x + 9$

Difference of two squares:

$$(x-a)(x+a) = x_2 - a_2$$

 $(x-3)(x+3) = x_2 - 3_2$
 $= x_2 - 9$

EXERCISE B

Multiply out

- 1. $(x-1)^2$
- 2. (3x + 5)2
- 3. $(7x 2)^2$
- 4. (x+2)(x-2)
- 5. (3x+1)(3x-1)
- 6. (5y 3)(5y + 3)

More help:

Chapter 2: LINEAR EQUATIONS

When solving an equation, you must remember that whatever you do to one side must also be done to the other. You are therefore allowed to

- add the same amount to both side
- subtract the same amount from each side
- multiply the whole of each side by the same amount
- divide the whole of each side by the same amount.

If the equation has unknowns on both sides, you should collect all the letters onto the same side of the equation.

If the equation contains brackets, you should start by expanding the brackets.

A linear equation is an equation that contains numbers and terms in x. A linear equation does not contain any x^2 or x^3 terms.

More help on solving equations can be obtained by downloading the leaflet available at this website: http://www.mathcentre.ac.uk/resources/workbooks/mathcentre/web-simplelinear.pdf

Example 1: Solve the equation 64 - 3x = 25

$$64 - 3x = 25$$

Solution: There are various ways to solve this equation. One approach is as follows:

Step 1: Add 3x to both sides (so that the x term is positive):

$$64 = 3x + 25$$

Step 2: Subtract 25 from both sides:

$$39 = 3x$$

Step 3: Divide both sides by 3:

$$13 = x$$

So the solution is x = 13.

Example 2: Solve the equation 6x + 7 = 5 - 2x.

Solution:

Step 1: Begin by adding 2x to both sides

$$8x + 7 = 5$$

(to ensure that the *x* terms are together on the same side)

Step 2: Subtract 7 from each side:

$$8x = -2$$

Step 3: Divide each side by 8:

$$x = -\frac{1}{4}$$

Exercise A: Solve the following equations, showing each step in your working:

1)
$$2x + 5 = 19$$

2)
$$5x - 2 = 13$$

3)
$$11 - 4x = 5$$

4)
$$5 - 7x = -9$$

5)
$$11 + 3x = 8 - 2x$$

6)
$$7x + 2 = 4x - 5$$

Example 3: Solve the equation
$$2(3x - 2) = 20 - 3(x + 2)$$

Step 1: Multiply out the brackets:
$$6x - 4 = 20 - 3x - 6$$

Step 2: Simplify the right hand side:
$$6x - 4 = 14 - 3x$$

Step 3: Add 3x to each side:
$$9x - 4 = 14$$

Step 4: Add 4:
$$9x = 18$$

Step 5: Divide by 9:
$$x = 2$$

Exercise B: Solve the following equations.

1)
$$5(2x-4)=4$$

2)
$$4(2-x) = 3(x-9)$$

3)
$$8 - (x + 3) = 4$$

4)
$$14 - 3(2x + 3) = 2$$

More help:

https://vle.mathswatch.co.uk/vle/browse/297

EQUATIONS CONTAINING FRACTIONS

When an equation contains a fraction, the first step is usually to multiply through by the denominator of the fraction. This ensures that there are no fractions in the equation.

Example 4: Solve the equation
$$\frac{y}{2} + 5 = 11$$

Solution:

Step 1: Multiply through by 2 (the denominator in the fraction):
$$y + 10 = 22$$

Step 2: Subtract 10:
$$y = 12$$

Example 5: Solve the equation
$$\frac{1}{3}(2x+1) = 5$$

Solution:

Step 1: Multiply by 3 (to remove the fraction)
$$2x+1=15$$

Step 2: Subtract 1 from each side
$$2x = 14$$

Step 3: Divide by 2
$$x = 7$$

When an equation contains two fractions, you need to multiply by the lowest common denominator. This will then remove both fractions.

Example 6: Solve the equation
$$\frac{x+1}{4} + \frac{x+2}{5} = 2$$

Solution:

Step 1: Find the lowest common denominator:

The smallest number that both 4 and 5 divide into is 20.

Step 2: Multiply both sides by the lowest common denominator

$$\frac{20(x+1)}{4} + \frac{20(x+2)}{5} = 40$$

Step 3: Simplify the left hand side:

$$\frac{\cancel{20}(x+1)}{\cancel{4}} + \frac{\cancel{20}(x+2)}{\cancel{5}} = 40$$

$$5(x+1) + 4(x+2) = 40$$

Step 4: Multiply out the brackets:

$$5x + 5 + 4x + 8 = 40$$

Step 5: Simplify the equation:

$$9x + 13 = 40$$

Step 6: Subtract 13

$$9x = 27$$

Step 7: Divide by 9:

$$x = 3$$

Example 7: Solve the equation $x + \frac{x-2}{4} = 2 - \frac{3-5x}{6}$

Solution: The lowest number that 4 and 6 go into is 12. So we multiply every term by 12:

$$12x + \frac{12(x-2)}{4} = 24 - \frac{12(3-5x)}{6}$$

Simplify

$$12x + 3(x - 2) = 24 - 2(3 - 5x)$$

Expand brackets

$$12x + 3x - 6 = 24 - 6 + 10x$$

Simplify

$$15x - 6 = 18 + 10x$$

Subtract 10x

$$5x - 6 = 18$$

Add 6

$$5x = 24$$

Divide by 5

$$x = 4.8$$

Exercise C: Solve these equations

1)
$$\frac{1}{2}(x+3) = 5$$

2)
$$\frac{2x}{3} - 1 = \frac{x}{3} + 4$$

3)
$$\frac{y}{4} + 3 = 5 - \frac{y}{3}$$

4)
$$\frac{x-2}{7} = 2 + \frac{3-x}{14}$$

Exercise C (continued)

$$5) \qquad \frac{7x-1}{2} = 13 - x$$

6)
$$\frac{y-1}{2} + \frac{y+1}{3} = \frac{2y+5}{6}$$

7)
$$2x + \frac{x-1}{2} = \frac{5x+3}{3}$$

8)
$$2 - \frac{5}{x} = \frac{10}{x} - 1$$

More help:

https://vle.mathswatch.co.uk/vle/browse/385

FORMING EQUATIONS

Example 8: Find three consecutive numbers so that their sum is 96.

Solution: Let the first number be n, then the second is n + 1 and the third is n + 2.

Therefore

$$n + (n + 1) + (n + 2) = 96$$

$$3n + 3 = 96$$

$$3n = 93$$

$$n = 31$$

So the numbers are 31, 32 and 33.

Exercise D:

1) Find 3 consecutive even numbers so that their sum is 108.

2) The perimeter of a rectangle is 79 cm. One side is three times the length of the other. Form an equation and hence find the length of each side.

Two girls have 72 photographs of celebrities between them. One gives 11 to the other and finds that she now has half the number her friend has. Form an equation, letting *n* be the number of photographs one girl had at the **beginning**.

Hence find how many each has now.

Chapter 3: SIMULTANEOUS EQUATIONS

An example of a pair of simultaneous equations is 3x + 2y = 8 ①

5x + y = 11 ②

In these equations, x and y stand for two numbers. We can solve these equations in order to find the values of x and y by eliminating one of the letters from the equations.

In these equations it is simplest to eliminate y. We do this by making the coefficients of y the same in both equations. This can be achieved by multiplying equation ② by 2, so that both equations contain 2y:

3x + 2y = 8 ① 10x + 2y = 22 ② $2 \times ② = ③$

To eliminate the y terms, we subtract equation ③ from equation ①. We get: 7x = 14 i.e. x = 2

To find y, we substitute x = 2 into one of the original equations. For example if we put it into ②:

$$10 + y = 11$$
$$y = 1$$

Therefore the solution is x = 2, y = 1.

Remember: You can check your solutions by substituting both x and y into the original equations.

Example: Solve 2x + 5y = 16 ①

3x - 4y = 1 ②

Solution: We begin by getting the same number of x or y appearing in both equation. We can get 20y in both equations if we multiply the top equation by 4 and the bottom equation by 5:

8x + 20y = 64 ③ 15x - 20y = 5 ④

As the SIGNS in front of 20y are DIFFERENT, we can eliminate the y terms from the equations by ADDING:

23x = 69 ③+④ i.e. x = 3

Substituting this into equation ① gives:

6 + 5y = 165y = 10y = 2

So... y = 2

The solution is x = 3, y = 2.

If you need **more help** on solving simultaneous equations, you can download a booklet from the following website:

http://www.mathcentre.ac.uk/resources/workbooks/mathcentre/web-simultaneous1.pdf

Exercise:

Solve the pairs of simultaneous equations in the following questions:

$$x + 2y = 7
 3x + 2y = 9$$

$$2) \qquad x + 3y = 0$$
$$3x + 2y = -7$$

$$3x - 2y = 4$$
$$2x + 3y = -6$$

4)
$$9x - 2y = 25$$
$$4x - 5y = 7$$

5)
$$4a + 3b = 22$$

 $5a - 4b = 43$

6)
$$3p + 3q = 15$$

 $2p + 5q = 14$

Chapter 4: FACTORISING

Common factors

We can factorise some expressions by taking out a common factor.

Example 1: Factorise 12x - 30

Solution: 6 is a common factor to both 12 and 30. We can therefore factorise by taking 6

outside a bracket:

12x - 30 = 6(2x - 5)

Example 2: Factorise $6x^2 - 2xy$

Solution: 2 is a common factor to both 6 and 2. Both terms also contain an x.

So we factorise by taking 2x outside a bracket.

 $6x^2 - 2xy = 2x(3x - y)$

Example 3: Factorise $9x_3y_2 - 18x_2y$

Solution: 9 is a common factor to both 9 and 18.

The highest power of x that is present in both expressions is x_2 .

There is also a y present in both parts.

So we factorise by taking 9x2y outside a bracket:

 $9x_3y_2 - 18x_2y = 9x_2y(xy - 2)$

Example 4: Factorise 3x(2x - 1) - 4(2x - 1)

Solution: There is a common bracket as a factor.

So we factorise by taking (2x-1) out as a factor.

The expression factorises to (2x-1)(3x-4)

Exercise A

Factorise each of the following

- 1) 3x + xy
- 2) $4x_2 2xy$
- 3) pq_2-p_2q
- 4) 3pq 9q2
- 5) $2x_3 6x_2$
- 6) 8a5b2 12a3b4
- 7) 5y(y-1) + 3(y-1)

Factorising quadratics

Simple quadratics: Factorising quadratics of the form $x^2 + bx + c$

The method is:

Step 1: Form two brackets $(x \dots)(x \dots)$

Step 2: Find two numbers that multiply to give c and add to make b. These two numbers get written at the other end of the brackets.

Example 1: Factorise $x_2 - 9x - 10$.

Solution: We need to find two numbers that multiply to make -10 and add to make -9. These numbers are -10 and 1.

Therefore $x_2 - 9x - 10 = (x - 10)(x + 1)$.

General quadratics: Factorising quadratics of the form $ax^2 + bx + c$

The method is:

Step 1: Find two numbers that multiply together to make ac and add to make b.

Step 2: Split up the bx term using the numbers found in step 1.

Step 3: Factorise the front and back pair of expressions as fully as possible.

Step 4: There should be a common bracket. Take this out as a common factor.

Example 2: Factorise $6x^2 + x - 12$.

Solution: We need to find two numbers that multiply to make $6 \times -12 = -72$ and add to make 1. These two numbers are -8 and 9.

Therefore,
$$6x^2 + x - 12 = 6x^2 - 8x + 9x - 12$$

= $2x(3x - 4) + 3(3x - 4)$ (the two brackets must be identical)
= $(3x - 4)(2x + 3)$

Difference of two squares: Factorising quadratics of the form $x^2 - a^2$

Remember that $x^2 - a^2 = (x + a)(x - a)$.

Therefore:
$$x^2 - 9 = x^2 - 3^2 = (x+3)(x-3)$$

$$16x^2 - 25 = (2x)^2 - 5^2 = (2x+5)(2x-5)$$

Also notice that:
$$2x^2 - 8 = 2(x^2 - 4) = 2(x + 4)(x - 4)$$

and
$$3x^3 - 48xy^2 = 3x(x^2 - 16y^2) = 3x(x + 4y)(x - 4y)$$

Factorising by pairing

We can factorise expressions like $2x^2 + xy - 2x - y$ using the method of factorising by pairing:

$$2x^2 + xy - 2x - y = x(2x + y) - 1(2x + y)$$
 (factorise front and back pairs, ensuring both brackets are identical)

$$= (2x + y)(x - 1)$$

https://vle.mathswatch.co.uk/vle/browse/323

Exercise B

Factorise

1)
$$x^2 - x - 6$$

2)
$$x^2 + 6x - 16$$

3)
$$2x^2 + 5x + 2$$

4)
$$2x^2 - 3x$$
 (factorise by taking out a common factor)

5)
$$3x^2 + 5x - 2$$

6)
$$2y^2 + 17y + 21$$

7)
$$7y^2 - 10y + 3$$

8)
$$10x^2 + 5x - 30$$

9)
$$4x^2 - 25$$

10)
$$x^2 - 3x - xy + 3y^2$$

11)
$$4x^2 - 12x + 8$$

12)
$$16m^2 - 81n^2$$

13)
$$4y^3 - 9a^2y$$

14)
$$8(x+1)^2 - 2(x+1) - 10$$

Chapter 5: CHANGING THE SUBJECT OF A FORMULA

We can use algebra to change the subject of a formula. Rearranging a formula is similar to solving an equation – we must do the same to both sides in order to keep the equation balanced.

Example 1: Make x the subject of the formula y = 4x + 3.

Solution:y = 4x + 3Subtract 3 from both sides:y - 3 = 4xDivide both sides by 4; $\frac{y-3}{4} = x$

So $x = \frac{y-3}{4}$ is the same equation but with x the subject.

Example 2: Make x the subject of y = 2 - 5x

Solution: Notice that in this formula the *x* term is negative.

y = 2 - 5xAdd 5x to both sides y + 5x = 2 (the x term is now positive)

Subtract y from both sides 5x = 2 - y

Divide both sides by 5 $x = \frac{2 - y}{5}$

Example 3: The formula $C = \frac{5(F-32)}{9}$ is used to convert between ° Fahrenheit and ° Celsius.

We can rearrange to make F the subject.

 $C = \frac{5(F-32)}{9}$

Multiply by 9 9C = 5(F - 32) (this removes the fraction)

Expand the brackets 9C = 5F - 160Add 160 to both sides 9C + 160 = 5FDivide both sides by 5 $\frac{9C + 160}{5} = F$

Therefore the required rearrangement is $F = \frac{9C + 160}{5}$.

Exercise A

Make *x* the subject of each of these formulae:

1) y = 7x - 1

 $2) y = \frac{x+5}{4}$

3) $4y = \frac{x}{3} - 2$

4) $y = \frac{4(3x-5)}{9}$

Rearranging equations involving squares and square roots

Example 4: Make x the subject of $x^2 + y^2 = w^2$

Solution:
$$x^2 + y^2 = w^2$$

Subtract
$$y^2$$
 from both sides: $x^2 = w^2 - y^2$ (this isolates the term involving x)

Square root both sides:
$$x = \pm \sqrt{w^2 - y^2}$$

Remember that you can have a positive or a negative square root. We cannot simplify the answer any more.

Example 5: Make a the subject of the formula $t = \frac{1}{4} \sqrt{\frac{5a}{h}}$

Solution:
$$t = \frac{1}{4} \sqrt{\frac{5a}{h}}$$

Multiply by 4
$$4t = \sqrt{\frac{5a}{h}}$$

Square both sides
$$16t^2 = \frac{5a}{h}$$

Multiply by
$$h$$
:
$$16t^2h = 5a$$

Divide by 5:
$$\frac{16t^2h}{5} = a$$

Exercise B:

Make t the subject of each of the following

1)
$$P = \frac{wt}{32r}$$

$$P = \frac{wt^2}{32r}$$

$$V = \frac{1}{3}\pi t^2 h$$

$$4) P = \sqrt{\frac{2t}{g}}$$

$$Pa = \frac{w(v-t)}{g}$$

$$6) r = a + bt^2$$

More help:

More difficult examples

Sometimes the variable that we wish to make the subject occurs in more than one place in the formula. In these questions, we collect the terms involving this variable on one side of the equation, and we put the other terms on the opposite side.

Example 6: Make t the subject of the formula a - xt = b + yt

Solution: a - xt = b + yt

Start by collecting all the t terms on the right hand side:

Add xt to both sides: a = b + yt + xt

Now put the terms without a *t* on the left hand side:

Subtract *b* from both sides: a-b = yt + xt

Factorise the RHS: a-b=t(y+x)

Divide by (y + x): $\frac{a - b}{y + x} = t$

So the required equation is $t = \frac{a - b}{y + x}$

Example 7: Make W the subject of the formula $T - W = \frac{Wa}{2h}$

Solution: This formula is complicated by the fractional term. We begin by removing the fraction:

Multiply by 2b: 2bT - 2bW = Wa

Add 2bW to both sides: 2bT = Wa + 2bW (this collects the W's together)

Factorise the RHS: 2bT = W(a + 2b)

Divide both sides by a + 2b: $W = \frac{2bT}{a + 2b}$

If you need more help you can download an information booklet on rearranging equations from the following website:

http://www.mathcentre.ac.uk/resources/workbooks/mathcentre/web-formulae2-tom.pdf

https://vle.mathswatch.co.uk/vle/browse/358

Exercise C

Make *x* the subject of these formulae:

1) ax+3=bx+c 2) 3(x+a)=k(x-2)

3) $y = \frac{2x+3}{5x-2}$ 4) $\frac{x}{a} = 1 + \frac{x}{b}$

Chapter 6: SOLVING QUADRATIC EQUATIONS

A quadratic equation has the form $ax^2 + bx + c = 0$.

There are two methods that are commonly used for solving quadratic equations:

- * factorising
- * the quadratic formula

Note that not all quadratic equations can be solved by factorising. The quadratic formula can always be used however.

Method 1: Factorising

Make sure that the equation is rearranged so that the right hand side is 0. It usually makes it easier if the coefficient of x_2 is positive.

Example 1: Solve $x_2 - 3x + 2 = 0$

$$(x-1)(x-2) = 0$$

Either
$$(x-1) = 0$$
 or $(x-2) = 0$

So the solutions are
$$x = 1$$
 or $x = 2$

Note: The individual values x = 1 and x = 2 are called the **roots** of the equation.

Example 2: Solve $x_2 - 2x = 0$

$$x(x-2) = 0$$

Either
$$x = 0$$
 or $(x - 2)' = 0$

So
$$x = 0$$
 or $x = 2$

https://vle.mathswatch.co.uk/vle/browse/360

Method 2: Using the formula

Recall that the roots of the quadratic equation $ax^2 + bx + c = 0$ are given by the formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Example 3: Solve the equation $2x^2 - 5 = 7 - 3x$

Solution: First we rearrange so that the right hand side is 0. We get $2x^2 + 3x - 12 = 0$

We can then tell that a = 2, b = 3 and c = -12.

Substituting these into the quadratic formula gives:

$$x = \frac{-3 \pm \sqrt{3^2 - 4 \times 2 \times (-12)}}{2 \times 2} = \frac{-3 \pm \sqrt{105}}{4}$$
 (this is the *surd form* for the solutions)

If we have a calculator, we can evaluate these roots to get: x = 1.81 or x = -3.31

If you need more help with the work in this chapter, there is an information booklet downloadable from this web site:

http://www.mathcentre.ac.uk/resources/workbooks/mathcentre/web-quadraticequations.pdf

EXERCISE

- 1) Use factorisation to solve the following equations:
- a) $x_2 + 3x + 2 = 0$

b) $x_2 - 3x - 4 = 0$

- c) $x_2 = 15 2x$
- 2) Find the roots of the following equations:
- a) $x_2 + 3x = 0$

b) $x_2 - 4x = 0$

- c) $4 x_2 = 0$
- 3) Solve the following equations either by factorising or by using the formula:
- a) $6x_2 5x 4 = 0$

b) $8x_2 - 24x + 10 = 0$

- 4) Use the formula to solve the following equations to 3 significant figures. Some of the equations can't be solved.
- a) $x_2 + 7x + 9 = 0$

b) $6 + 3x = 8x_2$

c) $4x_2 - x - 7 = 0$

d) $x_2 - 3x + 18 = 0$

e) $3x_2 + 4x + 4 = 0$

f) $3x_2 = 13x - 16$

Chapter 7: INDICES

Basic rules of indices

 y^4 means $y \times y \times y \times y$.

4 is called the **index** (plural: indices), **power** or **exponent** of y.

There are 3 basic rules of indices:

$$1) a^m \times a^n = a^{m+n}$$

e.g.
$$3^4 \times 3^5 = 3^9$$

 $3^8 \times 3^6 = 3^2$

$$2) a^m \div a^n = a^{m-n}$$

e.g.
$$3^8 \times 3^6 = 3^2$$

$$(a^m)^n = a^{mn}$$

e.g.
$$(3^2)^5 = 3^{10}$$

Further examples

$$y^4 \times 5y^3 = 5y^7$$

 $4a^3 \times 6a^2 = 24a^5$

(multiply the numbers and multiply the a's)

 $2c^2 \times \left(-3c^6\right) = -6c^8$

(multiply the numbers and multiply the c's)

$$24d^7 \div 3d^2 = \frac{24d^7}{3d^2} = 8d^5$$

(divide the numbers and divide the d terms i.e. by subtracting

the powers)

Exercise A

Simplify the following:

1)
$$b \times 5b^5$$

(Remember that $b = b^1$)

2)
$$3c^2 \times 2c^5 =$$

3)
$$b^2c \times bc^3 =$$

4)
$$2n^6 \times (-6n^2) =$$

5)
$$8n^8 \div 2n^3 =$$

6)
$$d^{11} \div d^9 =$$

7)
$$\left(a^3\right)^2 =$$

8)
$$\left(-d^4\right)^3 =$$

Help:

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https://vle.mathswatch.co.uk/vle/browse/320 https://vle.mathswatch.co.uk/vle/browse/356

SOLUTIONS TO THE EXERCISES

CHAPTER 1:

Ex A

1)
$$28x + 35$$

2)
$$-15x + 21$$

3)
$$-7a + 4$$

4)
$$6y + 3y_2$$

5)
$$2x-4$$

6)
$$7x - 1$$

7)
$$x_2 + 5x + 6$$

8)
$$t_2 - 3t - 10$$

9)
$$6x_2 + xy - 12y_2$$

10)
$$4x_2 + 4x - 24$$

$$x_2 + 4x - 24$$
 11) $4y_2 - 1$

12)
$$12 + 17x - 5x_2$$

Ex B

1)
$$x_2 - 2x + 1$$

2)
$$9x_2 + 30x + 25$$

3)
$$49x_2 - 28x + 4$$
 4) $x_2 - 4$

4)
$$x_2 - 4$$

5)
$$9x_2 - 1$$

6)
$$25y_2 - 9$$

CHAPTER 2

Ex A

Ex B

Ex C

1) 34, 36, 38 2) 9.875, 29.625 3) 24, 48

CHAPTER 3

1)
$$x = 1, y = 3$$

1)
$$x = 1, y = 3$$
 2) $x = -3, y = 1$ 3) $x = 0, y = -2$ 4) $x = 3, y = 1$

5)
$$a = 7$$
, $b = -26$) $p = 11/3$, $q = 4/3$

CHAPTER 4

Ex A

1)
$$\nu(2)$$

1)
$$x(3+y)$$
 2) $2x(2x-y)$ 3) $pq(q-p)$ 4) $3q(p-3q)$ 5) $2x_2(x-3)$ 6) $4a_3b_2(2a_2-3b_2)$

3)
$$pq(q-p)$$

4)
$$3q(p-3q)$$

5)
$$2x_2(x-3)$$

6)
$$4a_3b_2(2a_2-3b_2)$$

7)
$$(y-1)(5y+3)$$

Ex B

1)
$$(x-3)(x+2)$$

2)
$$(x + 8)(x - 2)$$

1)
$$(x-3)(x+2)$$
 2) $(x+8)(x-2)$ 3) $(2x+1)(x+2)$ 4) $x(2x-3)$ 5) $(3x-1)(x+2)$

4)
$$x(2x-3)$$

5)
$$(3x-1)(x+2)$$

6)
$$(2y+3)(y+7)$$
 7) $(7y-3)(y-1)$ 8) $5(2x-3)(x+2)$ 9) $(2x+5)(2x-5)$ 10) $(x-3)(x-y)$ 11) $4(x-2)(x-1)$ 12) $(4x-9x)(4x+9x)$ 13) $y(2y-3x)(2y+3x)$ 14) $2(4x+5)(x-4)$

11)
$$4(x-2)(x-1)$$
 12) $(4m-9n)(4m+9n)$ 13) $y(2y-3a)(2y+3a)$ 14) $2(4x+5)(x-4)$

13)
$$y(2y-3a)(2y+3a)$$

14)
$$2(4x+5)(x-4)$$

CHAPTER 5

Ex A

$$1) \quad x = \frac{y+1}{7}$$

2)
$$x = 4y - 5$$

1)
$$x = \frac{y+1}{7}$$
 2) $x = 4y-5$ 3) $x = 3(4y+2)$ 4) $x = \frac{9y+20}{12}$

4)
$$x = \frac{9y + 2y}{12}$$

Ex B

1)
$$t = \frac{32rP}{W}$$

1)
$$t = \frac{32rP}{w}$$
 2) $t = \pm \sqrt{\frac{32rP}{w}}$ 3) $t = \pm \sqrt{\frac{3V}{\pi h}}$ 4) $t = \frac{P^2g}{2}$ 5) $t = v - \frac{Pag}{w}$ 6) $t = \pm \sqrt{\frac{r-a}{b}}$

$$3) \ t = \pm \sqrt{\frac{3V}{\pi h}}$$

$$4) t = \frac{P^2 g}{2}$$

$$6) t = \pm 1$$

Ex C

$$1) \quad x = \frac{c-3}{a-b}$$

$$2) \quad x = \frac{3a + 2k}{k - 3}$$

1)
$$x = \frac{c-3}{a-b}$$
 2) $x = \frac{3a+2k}{k-3}$ 3) $x = \frac{2y+3}{5y-2}$ 4) $x = \frac{ab}{b-a}$

$$4) \quad x = \frac{ab}{b - a}$$

CHAPTER 6

CHAPTER 7

Ex A

$$) b_{3}c_{4}$$

1)
$$5b6$$
 2) $6c7$ 3) $b3c4$ 4) $-12n8$ 5) $4n5$ 6) $d2$ 7) $a6$ 8) $-d12$

$$8) -a$$